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# Comparative ab initio studies of heteroatom-doped carbon clusters $C_n X_p^+$ (X = P, S; n + p = 3-6)

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## Abstract

Theoretical studies of  $C_n X_p^+$  (X = P, S; n + p = 3-6) cations have been carried out. Predictions for their geometries and vibrational frequencies have been made using the B3LYP density functional method with both the 6-311G\* and aug-cc-pVTZ basis sets. Relative energies have been determined at ab initio high-quality electronic correlation level of theory (CCSD(T) and CISD). A comparison of the structures and stability show that the heteroatomic  $C_n X_p^+$  (n + p = 3, 4) clusters are unambiguously linear, except  $CX_3^+$ , for which we find a symmetric T-shaped ground-state structure with a central carbon atom. Regarding the homoatomic species,  $P_3^+$  is predicted to be cyclic, while  $S_3^+$  is bent,  $P_4^+$  possesses a puckered rhombic form, and  $S_4^+$  occurs as a square ring. When n + p = 5, 6, the cations  $C_n X_p^+$  (X = P, S) exhibit a wide range of forms as does the ground-state geometry (except the  $C_n X^+$  and  $C_n X_2^+$  compounds, which are invariably linear with the heteroatoms at the extremities). Building-up mechanisms in medium-sized mixed phosphorus– or sulfur–carbon compounds (n + p = 5, 6) are then suggested. The possible structural modifications caused by the charge of the heteroatom introduced in the cluster have been also explored. (Int J Mass Spectrom 206 (2001) 153–176) © 2001 Elsevier Science B.V.

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## 1. Introduction

During the past decade, much effort has been devoted to the elucidation of the structures and bonding of heteroatom-containing carbon clusters. Much of this interest is owing to, first, the development of various experimental techniques for both cluster formation and detection. For instance, mass spectrometry measurements of isolated clusters produced by laser vaporization of various carbide targets have led to the observation of a large number of anionic, for instance,  $C_n B^-$  [1] and  $C_n N^-$  [2], and cationic, as in  $C_n B_p^+$  [3] and  $C_n Si_p^+$  [4], species. A few chemical reactivity studies have been also devoted to  $C_n Si_p^+$  clusters [5,6]. However, laboratory spectroscopy in IR and millimeter or submillimeter regions is commonly used today for identification of neutral heteroatom-doped carbon clusters like  $C_n Si_p$  [7],  $C_n O$ [8], and  $C_n S$  [9].

Second, the rapid improvement in the accuracy and

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the feasibility of theoretical calculations has created interest. We can especially notice the increasing efficiency and availability of density functional codes with a superior cost-to-benefit ratio relative to other ab initio methodologies for medium and large size clusters [7,10,11].

Third, the discovery of a variety of carbon clusters bonded to heteroatom-like O [12], N [13], Si [14], and S [15] in circumstellar and interstellar media has also created interest, as has the recognition in fullerene research that substitution of a carbon fullerene by a foreign atom such as B, N, Si, or S provides a unique chemical environment that may induce significant change of the electronic properties and the possibility of new types of materials [3,4].

From a theoretical point of view, neutral [16] and cationic  $C_n Si_p$  [17] clusters have received a great deal of attention, even though the fact that carbon and silicon are in the same column (IV B) of the periodic table may constitute a very special case, indeed. However, very little is known regarding carbon clusters doped with other second-row elements. However, we have shown very recently that the cluster cation series  $C_n P^+$  [18] and  $C_n S^+$ [19] (n = 1-20) bear strong resemblance to the corresponding sequence of  $C_n Si^+$  cations [20]. In other words, the atomic structure, that is, the number of valence electrons, of the substitutional contaminant has only subtle effects on the groundstate geometry of pure carbon clusters doped with one single second-row atom. In binary systems, where carbons and second-row atoms are mixed in various proportions, the situation is, in contrast, much more intricate [16,17]. In the latter case, a theoretical comprehensive study appears to be eventually required. Thus, our aim is to present in this article a full survey of  $C_n X_p^+$  (X = P, S; n +p = 3-6) clusters in relation to  $C_n Si_p^+$  species. Emphasis will be given to the possible change in geometry caused by the charge of these clusters. The purpose of this work also is to provide theoretical data such as vibrational frequencies, dipole moments, and rotational constants to aid experimentalists and astrophysicists in detecting these transient molecules.

## 2. Methods

The computations were performed using the GAUSSIAN94 [21] package of programs implemented on an HP 9000/770 workstation. Two types of basis have been employed: the widely used Pople's 6-311G\* basis set [22] and the augmented Dunning correlation consistent valence triple  $\zeta$ ; (hereafter quoted as aug-cc-pVTZ) [23,24].

Methods used have been the density functional theory (DFT) with Becke's hybrid exchange functional [25]; correlation being treated through the Lee et al. functional [26] (following, it is referred to as B3LYP). Geometry optimizations for all the structures involved were made with this method by means of analytic gradient techniques. Vibrational frequencies were computed by fully analytic second-order derivatives. It has been proven that DFT/B3LYP agrees with more rigorous ab initio methods like CCSD(T) for geometries and spectra of carbon clusters but at very moderate cost [10].

We also used ab initio calculations for the accurate prediction of the relative energies on B3LYP/6-311G\* geometries employing the same basis set: First, the CCSD(T) level (coupled-cluster single- and double-excitation model augmented with a noniterative triple excitation correction) [27]. This method is known to yield results close to the exact n-particle solution within the given basis set, provided the system under consideration does not exhibit significant nondynamical correlation effect [28]. Second, the configuration interaction including all single and double excitations (CISD). These calculations have been performed to assess the reliability of single-referencebased methods. We found that the weight of the reference configuration in CISD treatment in all cases exceeds 0.91 and that the coefficient for the second configuration lies in the range 0.06-0.09. This fact suggests that the species under consideration  $(C_n P_p^+)$ and  $C_n S_p^+$ ) can be treated by single-reference-based computations.

Table 1

Relative energies, vibrational frequencies, Zero Point Energies (ZPE), dipole moments, and rotational constants (A, B, C) for  $C_n P_p^+$  (n + p = 3) structures optimized with B3LYP/6-311G\* method

Isomer	State	$\langle S^2 \rangle$	B3LYP/ 6-311G*	B3LYP/aug- cc-pVTZ	CCSD(T)	CISD	Vibrational frequencies (cm <sup>-1</sup> )	ZPE (kcal mol <sup>-1</sup> )	Dipole moment (Debye)	A, B, C (GHz)
$C_2^+$										
I	<sup>2</sup> B <sub>2</sub>	1.02	0.0	0.0	0.0	0.0	718 ( <i>a</i> <sub>1</sub> ) 1231 ( <i>b</i> <sub>2</sub> ) 1663 ( <i>a</i> <sub>1</sub> )	5.2	0.61	52.261 40.296
II	$^{2}A_{1}$	0.78	3.8	4.0	2.4	8.2	598 ( <i>b</i> <sub>2</sub> ) 1283 ( <i>a</i> <sub>1</sub> ) 1755 ( <i>a</i> <sub>1</sub> )	5.2	0.53	22.753 51.512 41.755
	251+	0.74	0.4	0.1	2.0	15.0	101 ( )d 1000 ( ) 4000 ( )	0.1	0.00	23.062
111	$^{2}\Sigma_{u}$	0.76	8.4	9.1	3.8	15.0	124 $(\pi_u)^{a}$ 1228 $(\sigma_g)$ 4903 $(\sigma_u)$	9.1	0.00	12.644
IV	$^{4}A'_{1}$	3.76	14.7	15.2	16.8	-0.0	1178 (a') 1178 (a') 1559 (a')	5.6	0.00	43.379 43.379
										21.689
C <sub>2</sub> P': V	${}^{1}\Sigma^{+}$	0.00	0.0	0.0	0.0	0.0	$132 (\pi)^{d} 880 (\sigma) 1832 (\sigma)$	4.2	2.37	6.422
VI	<sup>1</sup> A.	0.00	14.8	11.8	12.4	13.4	$200 (b_2) 944 (a_1) 1770 (a_1)$	4.2	1.62	51.744
	1									14.491
										11.321
VII	$^{3}A_{2}$	2.01	25.7	23.4	27.4	20.5	762 $(b_2)$ 767 $(a_1)$ 1539 $(a_1)$	4.4	0.84	47.566
	2									13.761
										10.674
VIII	$^{3}\Sigma^{+}$	2.06	26.9	26.1	31.5	23.9	220 ( <i>m</i> ) 309 ( <i>m</i> ) 812 ( <i>o</i> ) 1817 ( <i>o</i> )	4.5	0.30	6.390
$CP_2$ : IX	$^{2}\Pi_{g}$	0.78	0.0	0.0	0.0	0.0	185 $(\pi_u)$ 260 $(\pi_u)$ 622 $(\sigma_g)$ 1303 $(\sigma_u)$	3.4	0.00	3.117
Х	$^{2}A_{1}$	0.76	21.9	16.1	21.1	20.6	445 $(a_1)^{"}$ 900 $(b_2)$ 1021 $(a_1)$	3.4	1.03	30.571
										6.711
										5.503
XI	$4\Sigma_u^-$	3.84	64.0	63.7	60.2	64.0	262 $(\pi_u)^{d}$ 583 $(\sigma_g)$ 1037 $(\sigma_u)$	3.1	0.00	3.071
XII p+.	$^{2}\Pi$	0.81	96.7	92.9	96.4	92.7	$109i(\pi) \ 80i(\pi) \ 567(\sigma) \ 704(\sigma)$	1.8	1.50	3.739
XIII	$^{1}A_{1}^{\prime } \\$	0.00	0.0	0.0	0.0	0.0	481 (e') 481 (e') 648 (a' <sub>1</sub> )	2.3	0.00	7.322
3/13/	35'-	0.10	20.5	12.5	40.1	20.5	50 ( ) <sup>d</sup> 440 ( ) 404 ( )	1.5	0.00	3.661
XIV	تکر <sub>g</sub>	2.13	39.5	43.5	40.1	58.5	$59 (\pi_u)^2 449 (\sigma_g) 494 (\sigma_u)$	1.5	0.00	2.053
X٧	$^{r}A_{2}$	2.06	40.8	40.5	42.5	41.0	$250(b_2)$ $255(a_1)$ $589(a_1)$	1.0	0.24	9.418
										4.934
VVI	$1\Sigma^+$	0.00	617	613	62.2	60.9	20(-) $05(-)$ $472(-)$ $620(-)$	1.9	0.00	3.238
	∠g	0.00	01./	04.3	02.5	09.8	$50 (\pi_u) 95 (\pi_u) 4/2 (\sigma_g) 050 (\sigma_u)$	1.0	0.00	2.077

<sup>d</sup> Degenerate frequency.

Note. B3LYP/aug-cc-pVTZ, CCSD(T) and CISD energy differences are also given, respectively, in columns 5, 6, and 7. The numbering is according to Fig. 1.

## 3. Results and discussion

A number of structures have been optimized for each individual cation  $C_n P_p^+$  and  $C_n S_p^+$ . Tables 1, 2, 4, 5 list the electronic states, relative energies (at B3LYP, CCSD(T) and CISD levels), vibrational frequencies, zero-point-energy (ZPE), and rotational constants for the low-energy isomers of  $C_n X_p^+$  (X = P, S; n + p = 3, 4) clusters. The corresponding geometries are graphically shown in Figs. 1, 2, 5, and 6. The B3LYP relative energies for the various structures of cations  $C_n X_p^+$  (X = P, S; n + p = 5, 6) are included in Figs. 3, 4, 7, and 8. Other results for the latter species, not reported here, such as vibra-

Table 2

Relative energies, vibrational frequencies, Zero Point Energies (ZPE), dipole moments and rotational constants (A, B, C) for  $C_n P_p^+$  (n + p = 4) structures optimized with B3LYP/6-311G\* method

Isomer	State	$\langle S^2 \rangle$	B3LYP/ 6-311G*	CCSD(T)	Vibrational frequencies (cm <sup>-1</sup> )	ZPE (kcal mol <sup>-1</sup> )	Dipole moment (Debye)	A, B, C (GHz)	
C <sub>4</sub> <sup>+</sup> :	<sup>2</sup> П	0.76	0.0	0.00	$120(\pi)$ 138( $\pi$ ) 207( $\pi$ )	7.3	0.00	4 806	
Ι	g				$279 (\pi_g) 888 (\sigma_g) 1324 (\sigma_u)$				
II	${}^{4}\Sigma_{g}^{-}$	3.81	5.9	4.9	2141 $(\sigma_g)$ 300 <i>i</i> $(\pi_u)^d$ 450 $(\pi_g)^d$ 951 $(\sigma_g)$ 1901 $(\sigma_u)$	8.4	0.00	5.029	
III	${}^{2}\mathrm{B}_{1u}$	0.75	6.5	-3.2	2148 $(\sigma_g)$ 398 <i>i</i> $(b_{1u})$ 333 $(b_{3u})$ 610 $(b_{2u})$ 772 $(a_g)$	5.9	0.00	29.988	
					1146 $(b_{3g})$ 1279 $(a_g)$			15.488	
IV	${}^{4}B_{1}$	3.77	13.6	10.9	581 $(b_1)$ 766 $(b_2)$ 836 $(b_2)$ 877 $(a_1)$	8.4	0.00	36.318	
C D <sup>+</sup>					1387 ( <i>a</i> <sub>1</sub> ) 1460 ( <i>a</i> <sub>1</sub> )			15.708 10.965	
V	$^{3}\Sigma^{+}$	2.05	0.0	0.0	98 $(\pi)^{d}$ 330 $(\pi)^{d}$ 658 $(\sigma)$ 1255 $(\sigma)$ 1997 $(\sigma)$	6.8	2.45	2.743	
VI	$^{1}\Sigma^{+}$	0.00	18.3	11.8	$108 (\pi) 168 (\pi) 281 (\pi) 448 (\pi) 681 (\sigma) 1288 (\pi) 2000 (\pi) 1288 (\pi) 281 (\pi) 281 (\pi) (\pi) 281 (\pi) (\pi) (\pi) (\pi) (\pi) (\pi) (\pi) (\pi) (\pi) (\pi)$	7.1	2.69	2.749	
VII	<sup>3</sup> B <sub>1</sub>	2.01	20.5	12.3	$\begin{array}{c} 1288 (6) \ 2000 (6) \\ 419 (b_1) \ 430 (b_2) \ 623 (a_1) \\ 901 \ (a_1) \end{array}$	7.3	0.78	36.726	
VIII	<sup>1</sup> A <sub>1</sub>	0.00	32.7	29.8	1131 $(b_2)$ 1597 $(a_1)$ 240 <i>i</i> $(b_1)$ 375 $(b_2)$ 686 $(a_1)$ 1007 $(a_1)$ 1035 $(b_2)$ 1271 $(a_1)$	6.2	3.61	6.484 36.731 6.485	
$C \mathbf{p}^+$								5.512	
IX	$^{2}\Pi_{g}$	0.76	0.0	0.0	150 $(\pi_u)$ 166 $(\pi_u)$ 421 $(\pi_g)$ 480 $(\pi_g)$ 550 $(\sigma_g)$ 1172 $(\sigma_u)$	6.8	0.00	1.558	
Х	${}^{2}B_{1}$	0.76	29.1	22.9	$\begin{array}{c} 1810 \ (\sigma_g) \\ 295 \ (b_1) \ 396 \ (b_2) \ 547 \ (a_1) \\ 902 \ (b_2) \end{array}$	5.9	0.00	39.396	
					962 $(a_1)$ 1061 $(a_1)$			3.223	
XI	${}^{4}\Pi_{u}$	3.78	32.2	34.3	131 ( $\pi_u$ ) 140 ( $\pi_u$ ) 289 ( $\pi_g$ ) 376 ( $\pi_g$ )	6.0	0.00	1.473	
XII	<sup>2</sup> B <sub>1</sub>	0.75	51.5	50.4	479 $(\sigma_g)$ 808 $(\sigma_u)$ 1996 $(\sigma_g)$ 112 $(b_2)$ 234 $(b_1)$ 506 $(a_1)$ 584 $(b_2)$	5.3	2.49	7.532	
					712 $(a_1)$ 1539 $(a_1)$			5.715	
$CP_3^+$ :								3.250	
XIII	${}^{1}A_{1}$	0.00	0.0	0.00	112 $(b_2)$ 325 $(b_1)$ 427 $(a_1)$ 441 $(b_2)$	4.6	0.12	8.050	
					669 $(a_1)$ 1213 $(a_1)$			2.434	
							(continued on	next nage)	

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Table 2 (continued)

Isomer	State	$\langle S^2 \rangle$	B3LYP/ 6-311G*	CCSD(T)	Vibrational frequencies (cm <sup>-1</sup> )	ZPE (kcal mol <sup>-1</sup> )	Dipole moment (Debye)	A, B, C (GHz)
XIV	<sup>3</sup> A <sub>2</sub>	2.01	11.6	13.2	203 (b <sub>2</sub> )288 (b <sub>1</sub> )413 (a <sub>1</sub> ) 584 (a <sub>1</sub> )	4.6	1.08	7.341
					678 (b <sub>2</sub> )1046 (a <sub>1</sub> )			2.433
	1							1.827
XV	$\Sigma^{+}$	0.00	18.1	17.4	$\begin{array}{c} 63 \ (\pi)^{a} 247 \ (\pi)^{a} 457 \ (\sigma) \\ 855 \ (\sigma) 1490 \ (\sigma) \end{array}$	4.9	0.37	1.171
XVI	$^{1}A_{1}$	0.00	39.5	39.6	238 (e) <sup>d</sup> 313 ( $a_1$ )885 ( $e$ ) <sup>d</sup> 912 ( $a_1$ )	5.0	0.22	4.835
								4.835
								2.675
$P_{4}^{+}$ :	_							
XVII	${}^{2}B_{1}$	0.79	0.0	0.0	238 ( $a_1$ )301 ( $a_2$ )314 ( $a_1$ ) 439 ( $b_1$ )	3.2	0.64	4.354
					441 (b <sub>2</sub> )530 (a <sub>1</sub> )			2.900
								2.012
XVIII	${}^{2}B_{2}$	0.77	15.3	14.7	89 (b <sub>1</sub> )105 (b <sub>2</sub> )354 (a <sub>1</sub> ) 417 (b <sub>2</sub> )553 (a <sub>1</sub> )	3.1	0.50	7.454
					682 (a <sub>1</sub> )			1.589
								1.310
XIX	${}^{4}\mathrm{B}_{1u}$	3.76	25.0	24.0	166 (b <sub>3u</sub> )271 (a <sub>g</sub> )300 (b <sub>2u</sub> ) 372 (b <sub>1u</sub> )	3.0	0.00	4.547
					486 (b <sub>3g</sub> )491 (a <sub>g</sub> )			2.818
								1.739
XX	${}^{2}A_{2}$	0.77	26.6	38.0	$355i (b_1)207 (b_2)276 (b_2)$	2.8	0.00	6.112
					$413(a_1)$			2 5 2 9
					$519(a_1)538(a_1)$			2.528
								1./88

<sup>d</sup> Degenerate frequency.

Note. CCSD(T) energy differences are given in column 5. The numbering is according to Fig. 2.

tional frequencies and rotational constants are available on request.

## A. The $C_n P_p^+$ compounds

The  $C_2P^+$  cation is predicted to be unambiguously linear ( ${}^{1}\Sigma^+$ , structure V) with one CC double bond, ~1.33 Å, and one CP double bond, ~1.58 Å. The phosphorus bears the extra charge, and the submolecule  $C_2$  is quasineutral. On the contrary for  $C_2Si^+$ , Lavendy et al. [29] have found that the linear and cyclic isomers are energetically close to each other with insignificant energy separation of 0.1 kcal mol<sup>-1</sup> at MRCI level. This illustrates a distinct valence structure effect in  $C_2X^+$  depending on whether the heterotaom X is Si or P (Si and C share the same valence structure, while P, on the right of Si in the periodic table, has one additional electron). A similar conclusion can be made when comparing  $CP_2^+$  and  $CSi_2^+$ . As a matter of fact, we know that  $CSi_2^+$  is predicted to be cyclic but with an energetic separation to the linear of 0.5 kcal  $mol^{-1}$  at MRCI level [29]. Once again, as for  $C_2Si^+$ , this cation seems to hesitate between cyclic or linear geometry for its ground state. Besides, the lowest-energy  $CP_2^+$  isomer (structure IX) is unambiguously the linear arrangement of nuclei in the  ${}^{2}\Pi_{o}$  electronic state. Two double CP bonds  $(\sim 1.62 \text{ Å})$  are formed, and the carbon atom is in central position. The cyclic isomer  $(^{2}A_{1}, \text{ structure } X)$ is located above the linear one, (structure IX) respectively, by  $\sim$ 21.9 kcal mol<sup>-1</sup> at B3LYP and 21.1 kcal  $mol^{-1}$  at CCSD(T) levels. The latter structure is a

Table 3. Building-up patterns of the  $C_n P_p^+$  (n + p = 5, 6) clusters in their ground state. The various structures, optimized with the B3LYP/6-311G\* method are reproduced in Figs. 3 and 4.

	$\Delta E_b$ (eV)
$CP_2^+(\text{linear}, {}^2\Pi_e) + CP({}^2\Sigma^+) \leftarrow C_2P_3^+(X, {}^1A')$	5.38
$C_2P(\text{linear, }^2\Pi) + P_2(^1\Sigma_{e}^+) \leftrightarrow C_2P_3^+(X, ^1A')$	4.23
$CP_2(linear, {}^{3}\Sigma_{g}^{-}) + P_2^{+}({}^{2}\Sigma_{g}^{+}) \leftrightarrow CP_4^{+}(XIV, {}^{2}B_1)$	3.31
$P_3^+(\text{cyclic}, {}^{1}A_1') + P_2({}^{1}\Sigma_g^+) \leftrightarrow P_5^+(\text{XVIII}, {}^{1}A_1)$	1.48
$C_3P_2^+(\text{linear}, {}^2\Pi_u) + P({}^4S) \leftrightarrow C_3P_3^+(XII, {}^1A_1)$	3.31
$CP_2(linear, {}^{3}\Sigma_{g}) + CP_2^{+}(linear,$	3.00
${}^{2}\Pi_{g}) \leftrightarrow C_{2}P_{4}^{+}(XVI, {}^{2}A_{u})$	
$CP(^{2}\Sigma^{+}) + P_{4}^{+}$ (puckered rhombus,	4.50
$^{2}B_{1}) \leftrightarrow CP_{5}^{+}(XX, {}^{1}A')$	
$CP_3^+(T-shaped, {}^{1}A_1) + P_2({}^{1}\Sigma_g^+) \leftrightarrow CP_5^+(XX,$	1.56
<sup>1</sup> A')	
$P_3^+(\text{cyclic}, {}^1A_1') + P_3(\text{linear}, {}^2\Pi_p) \leftrightarrow P_6^+(XXIV,$	2.59
$^{2}A_{g})$	

Note. B3LYP/6-311G\* total energies for P(<sup>4</sup>S), E = -341.280483; CP(<sup>2</sup>Σ<sup>+</sup>), E = -379.328445; CP(<sup>3</sup>Π), E = -378.928684; CP<sub>2</sub>(<sup>3</sup>Σ<sub>g</sub><sup>-</sup>), E = -720.788533; CP<sub>2</sub>(<sup>2</sup>Π<sub>g</sub>), E = -720.464572; C<sub>2</sub>P(<sup>2</sup>Π), E = -417.411929; P<sub>2</sub>(<sup>1</sup>Σ<sub>g</sub><sup>+</sup>), E = -682.734019; P<sub>2</sub>(<sup>2</sup>Σ<sub>g</sub><sup>+</sup>), E = -682.335715.  $\Delta E_b$  denotes the binding energy of the cluster viewed as composed of two submolecules listed in the first column.

local minimum (all real frequencies) on the  $CP_2^+$ energy surface. The next species in the  $C_n P_p^+$  sequence is  $P_3^+$ . This time, the linear-cyclic energy ordering is reversed, and this cation is clearly cyclic in its ground state ( ${}^{1}A'_{1}$ , structure XIII), lying  $\sim$  39.5 kcal  $mol^{-1}$  at B3LYP and 40.1 kcal  $mol^{-1}$  at CCSD(T) levels under the linear  ${}^{3}\Sigma_{g}^{-}$ . It is worthy to note that  $P_3^+$  is a perfect equilateral triangle (<sup>1</sup>A<sub>1</sub>', structure XIII) with an equal charge (+e/3) distributed on each phosporus. We can notice that compared to the linear, the cyclic configuration has one additional PP bond. The building up of the tetra-atomic structures (Fig. 2) from the triatomic ones (Fig. 1) is straightforward. The ground-state geometries of the cations  $C_3P^+$  $({}^{3}\Sigma^{+}$ , structure V) and  $C_{2}P_{2}^{+}$  ( ${}^{2}\Pi_{g}$ , structure IX) are derived from the linear  $C_2 P^+$  ( $^1\Sigma^{\circ+}$ , structure V) by, respectively, adding either a carbon or a phosphorus atom to the CC moiety. One way to build up  $CP_3^+$  is to add a phosphorus to the linear  $CP_2^+$ . Proceeding like this, however, leads to a linear cluster with one PP double bond, which is found to be energetically less favorable than a CP bond. Another pathway is, thus, to start from the cyclic  $CP_2^+$ . This time, sticking a supplementary phosphorus to carbon gives a Tshaped configuration (<sup>1</sup>A<sub>1</sub>, structure XIII) with three CP bonds. In the latter structure, the carbon atom is negatively charged and the three phosphorus atoms

around it are positively charged with quasiequal charges (Fig. 2), minimizing the electrostatic energy. The T-shaped  $CP_3^+$  is located under the linear by  $\sim$ 18.1 kcal mol<sup>-1</sup> at B3LYP and 17.4 kcal mol<sup>-1</sup> at CCSD(T) levels, respectively. Both of these isomers, with all real frequencies, are local minima on the  $CP_3^+$ energy surface. A very similar operation can be performed on  $P_3^+$  and leads to a T-shaped  $P_4^+$ . However, this isomer is found to be less stable than the puckered rhombus ( ${}^{2}B_{1}$ , structure XVII) by 15.3 kcal  $mol^{-1}$  at the B3LYP level and 14.7 kcal  $mol^{-1}$  at the CCSD(T) level. We can notice that in the case of the neutral P<sub>4</sub>, a tetrahedral configuration was predicted for the ground state [30]. This indicates that the extra charge destabilizes the  $T_d$  arrangement of nuclei toward a lower symmetry  $(C_{2\nu})$ . Such a symmetry breaking was already encountered in C<sub>n</sub>Si<sub>p</sub> clusters [17].

Some general remarks for the energetics in  $C_n P_p^+$ compounds can be deduced from Tables 1 and 2. First, we can notice the good agreement between B3LYP and CCSD(T) energy differences for the heteroatomic clusters with maximal energy deviation systematically <10 kcal mol<sup>-1</sup> between these two levels of energy computation. However, B3LYP seems to be less dependable for the evaluation of relative energies in the homoatomic species. As has Table 4

Relative energies, vibrational frequencies, Zero Point Energies (ZPE), dipole moments and rotational constants (A, B, C) for  $C_n S_p^+$  (n + p = 3) structures optimized with B3LYP/6-311G\* method

Isomer	State	$\langle S^2 \rangle$	B3LYP/ 6-311G*	B3LYP/aug -cc-pVTZ	CCSD(T)	CISD	Vibrational frequencies (cm <sup>-1</sup> )	ZPE (kcal mol <sup>-1</sup> )	Dipole moment (Debye)	A, B, C (GHz)
$C_2S^+$ :										
I	$^{2}\Pi$	0.76	0.0	0.0	0.0	0.0*	182 ( $\pi$ ) 252 ( $\pi$ ) 858 ( $\sigma$ ) 1577 ( $\sigma$ )	4.1	1.11	6.422
II	$4\Sigma^{-}$	3.81	1.3	1.3	3.0	14.6*	360 (π) 905 (σ) 1701 (σ)	4.7	1.35	6.667
III	$^{2}B_{2}$	0.75	27.9	25.0	29.4	51.0*	$637i(b_2)$ 857 $(a_1)$ 1393 $(a_1)$	3.2	1.16	44.958
	2									15.338
										11.436
IV	${}^{4}A_{2}$	3.76	35.0	40.0	36.0	51.9*	$480 (b_2) 699 (a_1) 1668 (a_1)$	4.1	0.33	49.862
	2						. 2, . 1, . 1,			12.807
										10.190
$CS_{2}^{+}:$										
v	$^{2}\Pi_{g}$	0.78	0.0	0.0	0.0	0.0	314 $(\pi_u)$ 365 $(\pi_u)$ 667 $(\sigma_g)$ 1247 $(\sigma_u)$	3.7	0.00	3.251
VI	$^{2}A_{2}$	0.77	65.7	58.4	63.9	65.0	$407 (b_2) 564 (a_1) 837 (a_1)$	2.6	1.41	23.554
	2									7.581
										5.735
VII	${}^{4}\Pi_{g}$	3.78	77.8	76.3	80.5	76.1	422 <i>i</i> ( $\pi_u$ ) 250 ( $\pi_u$ ) 580 ( $\sigma_g$ ) 1282 ( $\sigma_u$ )	3.0	0.00	3.041
VIII	${}^{4}B_{2}$	3.76	103.8	96.8	103.7	93.3	$494(a_1)$ 752 (b <sub>2</sub> ) 913 (a <sub>1</sub> )	3.1	0.42	26.276
	2									7.219
										5.663
$S_{3}^{+}$										
IX	${}^{2}B_{2}$	0.76	0.0	0.0	0.0	0.0	209 $(a_1)$ 441 $(b_2)$ 598 $(a_1)$	1.8	0.60	15.445
										3.435
										2.810
Х	${}^{4}A_{1}$	3.76	7.0	9.6	9.3	8.0	215 $(a_1)$ 410 $(b_2)$ 564 $(a_1)$	1.7	0.00	10.150
										4.173
										2.957
XI	$^{2}\Sigma_{g}^{+}$	0.76	31.3	32.2	30.3	33.6	976 <i>i</i> $(\pi_u)^{d}$ 431 $(\sigma_g)$ 492 $(\sigma_u)$	1.3	0.00	2.059
XII	${}^{4}\Sigma_{u}^{+}$	3.91	56.0	54.2	50.1	54.8	550 $i(\pi_u)$ 465 $i(\sigma_u)$ 154 $(\pi_u)$ 326 $(\sigma_g)$	0.7	0.00	1.780

\* Geometry optimized at CISD level.

<sup>d</sup> Degenerate frequency.

Note. B3LYP/Aug-cc-pVTZ, CCSD(T) and CISD energy differences are also given, respectively in columns 5, 6 and 7. The numbering is according to Fig. 5.

already been noticed for  $C_4^+$  [31], the energy order for the linear  ${}^2\Pi_g$  and cyclic  ${}^2B_{1u}$  isomers found at B3LYP is reversed at CCSD(T) level. But these two isomers are energetically close to each other (energy separation of the order of 6 kcal mol<sup>-1</sup> at B3LYP level in favor of the linear and 3 kcal mol<sup>-1</sup> in favor of the cyclic at the CCSD(T) level of theory). For such a critical case, the CCSD(T) energies have to be considered more reliable than B3LYP ones [11].

Another major point of our study concerns the

deduction of the building-up patterns operative for large phosphorus–carbon clusters. This important element can be extracted from an analysis of the two consecutive sequences  $C_5^+$ ,  $C_4P^+$ ,...,  $P_5^+$  and  $C_6^+$ ,  $C_5P^+$ ,...,  $P_6^+$  when C is gradually replaced by P (Figs. 3, 4; Table 3). A general rule is that CC bonds are favored over CP bonds and PP bonds are—if possible—avoided to arrange the structures in a minimal energy state. A very similar conclusion was made by Froudakis et al. concerning the  $C_nSi_p$  clusTable 5

Relative energies, vibrational frequencies, Zero Point Energies (ZPE), dipole moments and rotational constants (A, B, C) for  $C_n S_p^+$  (n + p = 4) structures optimized with B3LYP/6-311G\* method

Isomer	State	$\langle S^2 \rangle$	B3LYP/ 6-311G*	CCSD(T)	Vibrational frequencies (cm <sup>-1</sup> )	ZPE (kcal mol <sup>-1</sup> )	Dipole moment (Debye)	A, B, C (GHz)
$C S^+$								
L <sup>3</sup> 2 :	$^{2}\Pi$	0.78	0.0	0.0	154 ( $\pi$ ) 190 ( $\pi$ ) 453 ( $\sigma$ ) 536 ( $\Pi$ ) 725 ( $\sigma$ ) 1363 ( $\sigma$ ) 1890 ( $\sigma$ )	7.6	1.58	2.834
II	<sup>2</sup> B <sub>1</sub>	0.77	35.4	32.7	472 $i$ ( $b_2$ ) 430 ( $b_2$ ) 674 ( $a_1$ ) 960 ( $b_1$ ) 1206 ( $a_1$ ) 1540 ( $a_1$ )	6.9	0.74	48.337 4.366
III	<sup>2</sup> A <sub>1</sub>	0.76	43.7	37.4	343 $(b_2)$ 374 $(b_1)$ 652 $(a_1)$ 957 $(a_1)$ 1028 $(b_2)$ 1686 $(a_1)$	7.2	0.07	4.004 37.114 6.779 5.732
IV	$4\Sigma^+$	3.80	46.4	57.7	107 ( $\pi$ ) 184 ( $\pi$ ) 376 ( $\pi$ ) 435 ( $\pi$ ) 696 ( $\sigma$ ) 1335 ( $\sigma$ ) 1981 ( $\sigma$ )	7.3	1.85	2.832
$C_{-}S^{+}$								
V	$^{2}\Pi_{u}$	0.75	0.0	0.0	176 $(\pi_u)$ 185 $(\pi_u)$ 361 $(\pi_g)$ 516 $(\pi_g)$ 579 $(\sigma_e)$ 1330 $(\sigma_u)$ 1900 $(\sigma_e)$	7.2	0.00	1.598
VI	${}^{4}\Pi_{g}$	3.76	41.7	44.6	157 $(\pi_u)$ 164 $(\pi_u)$ 284 $(\pi_g)$ 336 $(\pi_g)$ 520 $(\sigma_g)$ 812 $(\sigma_u)$ 1053 $(\sigma_g)$	6.2	0.00	1.520
VII	<sup>2</sup> A <sub>2</sub>	0.76	102.8	100.0	134 $(b_2)$ 251 $(b_1)$ 409 $(b_2)$ 526 $(a_1)$ 696 $(a_1)$ 1679 $(a_1)$	5.3	2.64	7.713 5.694 3.276
VIII	<sup>2</sup> B <sub>2</sub>	0.76	105.6	99.8	474 $i$ ( $b_1$ ) 192 ( $b_2$ ) 398 ( $a_1$ ) 472 ( $b_2$ ) 788 ( $a_1$ ) 877 ( $a_1$ )	3.9	0.00	34.028 3.249 2.966
CS <sub>3</sub> <sup>+</sup> : IX	${}^{2}B_{2u}$	0.76	0.0	0.0	213 $(b_2)$ 323 $(b_1)$ 341 $(b_2)$ 456 $(a_1)$ 604 $(a_1)$ 1299 $(a_1)$	4.6	2.01	7.441 2.529
Х	$^{4}\Sigma^{+}$	3.76	25.3	26.1	150 $(\pi)^{d}$ 94 $(\sigma)$ 289 $(\pi)^{d}$ 662 $(\sigma)$ 1464 $(\sigma)$	4.0	2.94	0.857
XI	$^{2}\Pi$	0.77	44.1	51.0	$550i (\pi) 434i (\pi) 198 (\pi) 205 (\pi) 332 (\sigma) 726 (\sigma) 1530 (\sigma)$	4.3	0.06	1.142
XII	<sup>4</sup> A <sub>1</sub>	3.76	50.2	52.4	379 $i$ ( $b_1$ ) 206 ( $b_2$ ) 423 ( $a_1$ ) 585 ( $b_2$ ) 594 ( $a_1$ ) 1115 ( $a_1$ )	4.2	1.76	7.622 2.408 1.830
S <sub>4</sub> <sup>+</sup> : XIII	<sup>2</sup> B <sub>1</sub>	0.75	0.0	0.0	72 $({}^{b}2_{u})$ 304 $({}^{b}1_{g})$ 450 $(e_{u})$ 450 $(e_{u})$ 497 $({}^{a}1_{g})$ 541 $({}^{b}2_{g})$	3.3	0.00	3.543 3.538
XIV	<sup>2</sup> A <sub>1</sub>	0.78	7.8	6.4	82 $(a_1)$ 153 $(a_2)$ 234 $(b_2)$ 251 $(a_1)$ 613 $(b_2)$ 671 $(a_1)$	2.9	0.13	11.279
								1.182
XV	${}^{2}\Pi_{u}$	0.77	20.2	16.9	76 <i>i</i> ( $\pi_u$ ) 62 <i>i</i> ( $\pi_u$ ) 143 ( $\sigma_g$ ) 152 ( $\pi_g$ ) 221 ( $\pi$ ) 715 ( $\sigma$ ) 731 ( $\sigma$ )	2.8	0.00	0.662
XVI	<sup>2</sup> B <sub>2</sub>	0.75	28.1	26.1	$\begin{array}{c} 257 & (a_1) & 304 & (a_1) & 318 & (b_2) & 323 & (a_2) \\ 413 & (b_1) & 512 & (a_1) \end{array}$	3.1	0.19	3.985 2.947 2.067

<sup>d</sup> Degenerate frequency.

Note. CCSD(T) energy differences are given in column 5. The numbering is according to Fig. 6.

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Fig. 1. Equilibrium geometries of  $C_n P_p^+$  (n + p = 3) clusters at the B3LYP/6-311G\* level of theory. Distances are in Ångstroms and angles in degrees. Mulliken charge distributions are given in parentheses. B3LYP relative energies (in kcal mol<sup>-1</sup>) are displayed under each structure together with some features about the vibrational frequencies (r indicates that all the frequencies are real, i notices one imaginary frequency, 2i two imaginary frequencies, etc.). B3LYP/6-311G\* total energies (in hartree) are also reported under the global minimum of each compound.

ters [16]. When p = 1, 2, calculations predict a cumulenic linear structure for  $C_n P_p^+$  (n + p = 5, 6) clusters with phosphorus atoms in the terminal positions. Similar ground-state geometry structures were found in the case of  $C_n Si_p^+$  [17]. Conversely, as soon as p is equal or >3, the ground-state structures of  $C_n P_p^+$  (n + p = 5, 6) drastically differ from the corresponding ones already found for  $C_n Si_p^+$  [17]. As a matter of fact, phosphorus has three unpaired electrons in  $3_p$  orbitals that are available for bonding,

but the promotional energy  $3s \rightarrow 3d$  is small enough to allow *d* orbitals to participate in bonding and form a number of possible hybridized orbitals with various interbond angles, which ultimately leads to many possible geometric arrangements [32].

The optimized structure of  $C_2P_3^+$  (<sup>1</sup>A', structure X) appears as a T-shaped configuration with a positive charge equally distributed at the periphery, that is, on the three phosphorus atoms. By contrast,  $C_2Si_3^+$  was found to be a Si-capped bent chain. As a consequence,



Α

Fig. 2. Equilibrium geometries of  $C_n P_p^+$  (n + p = 4) clusters at the B3LYP/6-311G\* level of theory. Distances are in Ångstroms and angles in degrees. Mulliken charge distributions are given in parentheses. B3LYP relative energies (in kcal mol<sup>-1</sup>) are displayed under each structure together with some features about the vibrational frequencies (r indicates that all the frequencies are real, i notices one imaginary frequency, 2i two imaginary frequencies, etc.). B3LYP/6-311G\* total energies (in hartree) are also reported under the global minimum of each compound.

the building-up pattern of these two clusters radically differs. Whereas  $C_2Si_3^+$  is formed by adding an Si atom perpendicularly to the median moiety ( $C_2$  submolecule) of the linear  $C_2Si_2^+$ , the cation  $C_2P_3^+$  (<sup>1</sup>A', structure X) is formed by placing a monopositive  $P_2$ fragment perpendicularly to a neutral  $C_2P$  submolecule, the latter one being taken in its linear <sup>2</sup>II ground state. Replacing a carbon atom by a phosphorus atom gives a planar  $CP_4^+$  cluster (<sup>2</sup>B<sub>1</sub>, structure XIV). The corresponding  $CSi_4^+$  cluster was found to be a C-capped quasiplanar  $Si_4^+$  structure. Again, even though these two clusters present some likeness, distinct building-up mechanisms have to be envisaged for them. The  $CSi_4^+$  cluster is formed by placing a carbon atom above a  $Si_4^+$  rhombus, while  $CP_4^+$  is formed by a cation  $P_2^+$  attached to a  $CP_2$  molecule in parallel. Likewise, the cation  $P_5^+$  is found to be a tetragonal pyramid (<sup>1</sup>A<sub>1</sub>, structure XVIII) with constrained interbond angles of 60°, whereas  $Si_5^+$  prefers a trigonal bipyramidal arrangement [17], the latter configuration being unstable for  $P_5^+$ . To the contrary, the tetragonal pyramidal arrangement was predicted to be a saddle point on the potential energy surface (PES) in the case of  $Si_5^+$  [17]. We can still notice that,



Fig. 2. (continued)

even though the tetragonal pyramidal configuration represents the ground-state geometry of P<sub>5</sub><sup>+</sup> (global minimum on the PES), this cation can easily be dissociated into a cation  $P_3^+$  and a  $P_2$  submolecule with very low fragmentation energy, of the order of 1.5 eV (Table 3). The building-up principle can also be extended to hexa-atomic clusters. The  $C_3P_3^+$  cluster adopts a T-shaped configuration ( ${}^{1}A_{1}$ , structure XII). This geometry can be viewed as a C<sub>3</sub>P linear chain with a cation  $P_2^+$  perpendicularly attached in terminal position on the opposite side to phosphorus. The geometry of  $C_2P_4^+$ , namely structure XVI, is formed by association of two symmetric CP2 submolecules strongly bound together by a double covalent CC bond with a positive charge equally distributed on the two  $CP_2$  moieties. Comparatively, the ground-state geometry of both neutral and cationic forms of C2Si4 was predicted to be the  $C_2$ -capped Si<sub>4</sub> rhombus [17]. The latter configuration is found to be unstable for  $C_2P_4^+$ . Exchanging now a carbon by a silicon gives  $CP_5^+$ . The ground-state geometry of this cluster (<sup>1</sup>A', structure XX) can be viewed as a puckered fourmembered ring  $P_4^+$  capped by a CP fragment placed perpendicularly above it. However, according to the binding energies listed in Table 3,  $CP_5^+$  appears as a T-shaped structure with three phosphorus atoms connected to a central sp<sup>2</sup>-hybridized carbon atom, the latter planar substructure being bridged by a P<sub>2</sub> submolecule placed perpendicularly to its plane. Again, this geometry is different from that found in  $CSi_5^+$ , which is a Si-capped quasiplanar  $CSi_4^+$  structure. Eventually,  $P_6^+$ , which looks like a puckered double-T-shaped arrangement of nuclei (<sup>2</sup>A<sub>g</sub>, structure XXIV), can be represented by two weakly interacting P<sub>3</sub> sharing a quasiequal positive charge. But this cation can easily dissociate into fragments P<sub>3</sub> and  $P_3^+$  with low fragmentation energy of the order of 2.6 eV (Table 3). In line with this, it is worth mentioning that  $Si_6^+$  prefers an edge-capped trigonal pyramid for its ground-state geometry [17].



Α

Fig. 3. Equilibrium geometries of  $C_n P_p^+$  (n + p = 5) clusters at the B3LYP/6-311G\* level of theory. Distances are in Ångstroms and angles in degrees. Mulliken charge distributions are given in parentheses. B3LYP relative energies (in kcal mol<sup>-1</sup>) are displayed under each structure together with some features about the vibrational frequencies (r indicates that all the frequencies are real, i notices one imaginary frequency, 2i two imaginary frequencies, etc.). B3LYP/6-311G\* total energies (in hartree) are also reported under the global minimum of each compound.

## B. The $C_n S_p^+$ compounds

We consider now how the mixed heteroatomcarbon clusters evolve when phosphorus is replaced by its neighbor to the right in the periodic table, that is, by sulfur, the latter element possessing a supplementary valence electron. Once again, as for  $C_nP^+$ and  $C_nP_2^+$ , the mono- and disulfide cations  $C_nS^+$  and  $C_nS_2^+$  are predicted to be cumulenic linear chains with CC and CS double bonds and S atoms in terminal positions (Figs. 5–8). This rule appears general for carbon clusters doped with one or two first-row or second-row elements. However, when three or more sulfur atoms are present in the cluster, the equilibrium structure drastically changes because of the fact that the cluster with three sulfur atoms refuses to adopt a linear geometry. For instance, the lowest-energy configuration of  $S_3^+$  is found to be a bent chain in the <sup>2</sup>B<sub>2</sub> electronic state (structure IX). In the latter structure, the two sulfur–sulfur bonds are ~1.96 Å, typical of relatively strong single sulfur–sulfur bonds (the sulfur–sulfur bond in H<sub>2</sub>S<sub>2</sub> is predicted to be on the order



Fig. 3. (continued)

of 2.06 Å, [33]; in contrast to  $P_3^+$ , however, the obtuse angle of 101.5° prevents the formation of an additional sulfur–sulfur bond to close the cycle). The linear isomer ( ${}^{2}\Sigma_{g}^{+}$ , structure XI) is located higher in energy above the bent configuration, at 31.3 kcal mol<sup>-1</sup> at B3LYP and 30.3 kcal mol<sup>-1</sup> at CCSD(T) levels. Moreover, the latter structure possesses one imaginary doubly degenerated bending mode, indicating that this configuration is not a local minimum on the S<sub>3</sub><sup>+</sup> energy surface. Adding a carbon to S<sub>3</sub><sup>+</sup>, we obtain CS<sub>3</sub><sup>+</sup>, which adopts a T-shaped configuration for its ground state ( ${}^{2}B_1$ , structure IX), with a carbon atom in the central position to realize the maximum number of CS bonds, that is, two single CS bonds (~1.80 Å) and one moderately strong double CS bond (~1.56 Å) (Fig. 6). The corresponding linear isomer ( ${}^{4}\Sigma^{+}$ , structure X) is located at about 25.3 kcal mol<sup>-1</sup> at the B3LYP level and 26.1 kcal mol<sup>-1</sup> at the CCSD(T) level above the T-shaped ground state. But this structure, with two imaginary frequencies, is a saddle point of higher order on the PES. Let us notice that the hypervalent pyramidal structure (not reported on Fig. 6) is located at 128.2 kcal mol<sup>-1</sup> above the absolute minimum, and the latter geometry also corrresponds to a saddle point on the PES. Adding now a sulfur atom to S<sub>3</sub><sup>+</sup> gives a S<sub>4</sub><sup>+</sup> square ring with four equivalent S atoms (<sup>2</sup>B<sub>2u</sub>, structure XIII). The next minimum on the PES of S<sub>4</sub><sup>+</sup> in the energetic ordering



Fig. 4. Equilibrium geometries of  $C_n P_p^+$  (n + p = 6) clusters at the B3LYP/6-311G\* level of theory. Distances are in Ångstroms and angles in degrees. Mulliken charge distributions are given in parentheses. B3LYP relative energies (in kcal mol<sup>-1</sup>) are displayed under each structure with some features about the vibrational frequencies (r indicates that all the frequencies are real, i notices one imaginary frequency, 2i two imaginary frequencies, etc.). B3LYP/6-311G\* total energies (in hartree) are also reported under the global minimum of each compound.

is the cis-planar structure XIV. This open form is found to lie only ~7.8 kcal mol<sup>-1</sup> above the squarering ground state. In contrast, the corresponding linear geometry ( ${}^{2}\Pi_{u}$ , structure XV), located at 20.1 kcal mol<sup>-1</sup> above the ground state, is not a minimum on the PES (two imaginary frequencies).

Regarding the energetics, as in the case of hetero-

atomic  $C_n P_p^+$  clusters, B3LYP and CCSD(T) energy differences for  $C_n S_p^+$  are in good agreement with each other, the maximal energy deviation being on the order of 5 kcal mol<sup>-1</sup> (there does, however, exist an exception in  $C_3 S^+$  where this deviation amounts to 10 kcal mol<sup>-1</sup> for the relative energies of the linear quadruplet  ${}^{4}\Sigma^{+}$  calculated with respect to the linear doublet



Fig. 4. (continued)



Fig. 5. Equilibrium geometries of  $C_n S_p^+$  (n + p = 3) clusters at the B3LYP/6-311G\* level of theory. Distances are in Ångstroms and angles in degrees. Mulliken charge distributions are given in parentheses. B3LYP relative energies (in kcal mol<sup>-1</sup>) are displayed under each structure together with some features about the vibrational frequencies (r indicates that all the frequencies are real, i notices one imaginary frequency, 2i two imaginary frequencies, etc.). B3LYP/6-311G\* total energies (in hartree) are also reported under the global minimum of each compound.

ground state). Comparatively, Martin et al. found much larger deviations in pure carbon clusters [11].

Special emphasis can be given to the bonding properties, especially the relationship between structure and stability for medium-sized mixed sulfurcarbon clusters, by examining the building-up mechanisms of  $C_n S_p^+$  (n + p = 5, 6) clusters (Figs. 7, 8; Table 6). However, as is usual for second-row heteroatom-doped carbon clusters when p = 1 or 2, we found a linear carbon chain with heteroatoms in terminal positions as ground-state geometry. Hence, we shall only discuss here the much more interesting case where  $p \ge 3$ . The planar  $C_2S_3^+$  cluster is composed of a cation  $CS_2^+$  with one CS bond capped by a CS molecule. Replacing one carbon by a sulfur atom gives a Van der Waals complex  $(CS_4^+)$  composed of two quasi-independent entities, CS2 and S2, with equal charge distributed on them. This result

demonstrates that the stability of carbon-doped sulfur molecules could indeed be relatively weak. The fragmentation energies of cations  $C_n S_p^+$  (n + p = 5, 6) have been summarized in Table 6, where we can see that these energies are very low, mostly on the order of 1-2.6 eV. Eventually, the ground-state geometry of the pure sulfur cluster  $S_5^+$  is a cis-trans open chain (<sup>2</sup>A", structure XV), which can readily decompose into  $S_3^+$  and  $S_2$  (Table 6). This structure is almost degenerate with the puckered ring (2A', structure XVI), with insignificant energetic separation  $\sim 0.1$ kcal  $mol^{-1}$  at B3LYP level. The corresponding cyclic planar isomer, with two imaginary frequencies, is a saddle point on the potential energy surface. Proceeding now to the hexa-atomic species (Fig. 8), the most favorable isomer of  $C_3S_3^+$  is represented by a fairly stable arrangement of nuclei, where each sulfur atom is bound on the periphery of a pure carbon submol-



Fig. 6. Equilibrium geometries of  $C_n S_p^+$  (n + p = 4) clusters at the B3LYP/6-311G\* level of theory. Distances are in Ångstroms and angles in degrees. Mulliken charge distributions are given in parentheses. B3LYP relative energies (in kcal mol<sup>-1</sup>) are displayed under each structure together with some features about the vibrational frequencies (r indicates that all the frequencies are real, i notices one imaginary frequency, 2i two imaginary frequencies, etc.). B3LYP/6-311G\* total energies (in hartree) are also reported under the global minimum of each compound.

ecule  $C_3$  (<sup>2</sup>B<sub>1</sub>, structure VIII). The next cluster,  $C_2S_4^+$ , obtained by replacing a carbon by a sulfur, is not a truly six-membered molecule but rather appears as two interacting, and equally charged,  $CS_2$  radicals. Hence, this metastable molecule can easily dissociate into a cation  $CS_2^+$  and the corresponding neutral

(Table 6). The global minimum of  $CS_5^+$  is predicted to be a five-membered puckered  $CS_4$  ring with an extra SC bond (<sup>2</sup>A', structure XV), but this form is isoenergetic with the distorted chain (<sup>2</sup>A<sub>1</sub>, structure XVI), the energy separation being insignificant (on the order of 1.5 kcal mol<sup>-1</sup> at the B3LYP/6-311G\* level).



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Fig. 7. Equilibrium geometries of  $C_n S_p^+$  (n + p = 5) clusters at the B3LYP/6-311G\* level of theory. Distances are in Ångstroms and angles in degrees. Mulliken charge distributions are given in parentheses. B3LYP relative energies (in kcal mol<sup>-1</sup>) are displayed under each structure with some features about the vibrational frequencies (r indicates that all the frequencies are real, i notices one imaginary frequency, 2i two imaginary frequencies, etc.). B3LYP/6-311G\* total energies (in hartree) are also reported under the global minimum of each compound.

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Fig. 8. Equilibrium geometries of  $C_n S_p^+$  (n + p = 6) clusters at the B3LYP/6-311G\* level of theory. Distances are in Ångstroms and angles in degrees. Mulliken charge distributions are given in parentheses. B3LYP relative energies (in kcal mol<sup>-1</sup>) are displayed under each structure with some features about the vibrational frequencies (r indicates that all the frequencies are real, i notices one imaginary frequency, 2i two imaginary frequencies, etc.). B3LYP/6-311G\* total energies (in hartree) are also reported under the global minimum of each compound.

Again, in these geometries, we can guess the association of two basic substructures, namely either  $(CS_3^+, S_2)$  or  $(S_3^+, CS_2)$  (Table 6). All these results can be rationalized by invoking that S easily partakes in double bonding with C rather than in linkage with other sulfur atoms, an effect that can ultimately break down a ring-shaped structure because the sulfur is essentially divalent in mixed carbon–sulfur clusters (the sulfur atom has six valence electrons but only two unpaired electrons, and the other two lone pairs do not participate into the bonding). Besides,  $S_6^+$  is a truly six-membered molecule ( $D_{3d}$  hexagonal chair) with





normal sulfur–sulfur single bond lengths (~2.10 Å). In a more general way, we can conjecture that the  $S_p^+$ (p = 4, 6, ...) ring-shaped structures appear to be formed from two weakly interacting submolecules and become unclosed configurations as soon as one sulfur atom is replaced by a carbon atom in the cycle. This is because of the formation of two relatively strong SC double bonds, which then preclude the neighboring sulfur atoms involved in these SC bonds from associating with other adjacent sulfurs to close the cycle.

### C. Geometry versus charge

The influence of the charge on geometry also deserves special attention because, in mass spectrometry, the clusters are ionized before analysis. Whether the cationic geometries can be expected to be relevant for the neutrals is thus an important question. For  $C_n Si_p$  (n + p = 5, 6), a comparison between the neutral and cationic forms clearly evidences that drastic change in the ground-state geometry can appear when the clusters are ionized. For instance,

Building-up patterns	of the	$C_{n}S_{n}^{+}$	(n +	p =	5, 6)	) clusters	in their	ground	state
		· • n • n	· · · ·	<i>r</i>	/			A	

	$\Delta E_b$ (eV)
$C_2S_2^+(\text{linear}, {}^2\Pi_{\rho}) + S({}^3P) \leftrightarrow C_2S_3^+(\text{VII}, {}^2A_1)$	2.06
$CS_{2}^{+}(\text{linear, }^{2}\Pi_{g})^{+} + CS(^{1}\Sigma^{+}) \leftrightarrow C_{2}S_{3}^{+}(VII,$ $^{2}A_{1})$	1.58
$CS_2(linear, {}^1\Sigma_g^+) + S_2^+({}^2\Pi_g) \leftrightarrow CS_4^+(XI, {}^2A_2)$	1.14
$S_3^+$ (bent, ${}^2B_2$ ) + $S_2({}^3\Sigma_g^-) \leftrightarrow S_5^+$ (XV, ${}^2A''$ )	1.59
$C_3S_2^+(\text{linear}, {}^2\Pi_u) + S({}^3P) \leftrightarrow C_3S_3^+(\text{VIII}, {}^2B_1)$	2.52
$C_2S_2^+(\text{linear}, {}^2\Pi_u) + CS({}^1\Sigma^+) \leftrightarrow C_3S_3^+(\text{VIII}, {}^2B_1)$	2.37
CS <sub>2</sub> <sup>+</sup> (linear, <sup>2</sup> Π <sub>g</sub> ) + CS <sub>2</sub> (linear, <sup>1</sup> Σ <sub>g</sub> <sup>+</sup> ) ↔ C <sub>2</sub> S <sub>4</sub> <sup>+</sup> (XII, <sup>2</sup> A <sub>g</sub> )*	-1.18
$ {}^{2}B_{2u} + CS(^{1}\Sigma^{+}) \leftrightarrow CS_{5}^{+}(XV, ^{2}A') $	2.59
$CS_3^+(T-shaped, {}^{2}B_1) + S_2({}^{3}\Sigma_g^-) \leftrightarrow CS_5^+(XV, {}^{2}A')$	1.66
$S_3^+$ (bent, ${}^2B_2$ ) + CS <sub>2</sub> (linear, ${}^1\Sigma_8^+$ ) ↔ CS <sub>5</sub> <sup>+</sup> (XV, ${}^2A'$ )	1.05
$S_3^+(\text{bent}, {}^2B_2) + S_3(\text{bent}, {}^1A_1) \leftrightarrow S_6^+(XIX, {}^2A_{1e})$	2.56
$S_2^+(^2\Pi_g) + ^2S_2(^3\Sigma_g^-) \leftrightarrow S_6^+(XIX, ^2A_{1g})$	2.40
$S_4^+(\text{square ring, }^2B_{2u}^-) + S_2(^3\Sigma_g^-) \leftrightarrow S_6^+(\text{XIX},$ $^2A_{1g})^2$	1.37

\* Metastable molecule.

Note. B3LYP/6-311G\* total energies for S(<sup>3</sup>P), E = -398.132082; CS(<sup>1</sup> $\Sigma^+$ ), E = -436.246153; CS<sub>2</sub>(<sup>1</sup> $\Sigma_g^+$ ), E = -834.550470; CS<sub>2</sub>(<sup>2</sup> $\Pi_g$ ), E = -834.178372; S<sub>2</sub>(<sup>3</sup> $\Sigma_g^+$ ), E = -796.412638; S<sub>2</sub>(<sup>2</sup> $\Pi_g$ ), E = -796.057392. The various structures, optimized with the B3LYP/6-311G\* method, are reproduced in Figs. 7 and 8.  $\Delta E_b$  denotes the binding energy of the cluster viewed as composed of the two submolecules listed in the first column.

C<sub>3</sub>Si<sub>3</sub> prefers a three-dimensional structure [16], while  $C_3Si_3^+$  adopts a Si-capped SiC<sub>3</sub>Si bent chain [17]. The role of the charge in the geometry is hereafter examined for the  $C_n P_p$  and  $C_n S_p$  clusters. We have determined the ground-state geometry (global minimum) of each neutral  $C_n X_n$  (X = P, S; n +p = 3-6) clusters. To do that, as usual, several possible alternative geometric arrangements have been optimized. The resulting geometries are displayed in Figs. 9 and 10, respectively for X = P and S. When ionized, the  $C_n X$  and  $C_n X_2$  species remain linear and tend toward the global minimum of the corresponding cation. Regarding the nonlinear forms, we find three categories: First, the geometry is not modified after ionization (if one excepts insignificant changes in the bond lengths and angles) and the ground-state geometries of both neutral and ionized structures are nearly identical. Such a situation is encountered in the mixed phosphorus-carbon clusters  $CP_3$ ,  $C_2P_3$ ,  $C_3P_3$ ,  $CP_4$ ,  $C_2P_4$ , and  $CP_5$ ; in the mixed

sulfur–carbon clusters  $CS_3$ ,  $C_2S_3$ , and  $CS_4$ ; and in the pure sulfur clusters  $S_3$  and  $S_6$ .

Second, the geometry remains unchanged after ionization but the related arrangement of nuclei does not represent the global minimum of the cationic congener. This occurs when the geometry adopted by the neutral species in its ground state corresponds to a local minimum on the PES of the cation. Thus,  $P_3$  is linear  $({}^{2}\Pi_{o})$ , but this configuration is metastable for  $P_3^+$  ( ${}^{3}\Sigma_{g}^-$ , structure XIV), being located at 39.5 kcal  $mol^{-1}$  above the ground state, namely a cyclic  $D_{3h}$ form  $({}^{1}A'_{1}$ , structure XIII). Likewise, such a situation also exists in sulfur compounds. The global minimum of S<sub>4</sub> is predicted to be a singlet cis planar structure [34-36]. This open chain also corresponds to a minimum on the PES of the cationic parent  $S_4^+$ , but the global minimum in the latter one is represented by a square ring  $({}^{2}B_{2\mu}$ , structure XIII), located under the cis open chain by 7.8 kcal  $mol^{-1}$ . A reverse situation appears in  $S_5$ . In the neutral  $S_5$ , the global minimum



Fig. 9. Ground state geometries of neutral  $C_n P_p$  (n + p = 3-6) clusters. B3LYP/6-311G\* total energies (in hartree) are displayed under each structure.

is a five-membered puckered ring, whereas in the related cation we find a cis-trans open chain (<sup>2</sup>A", structure XV) as ground state. In  $S_5^+$ , however, the energy separation between the open chain and the closed ring is found to be insignificant, on the order of 1 kcal mol<sup>-1</sup>, and these two states eventually appear almost degenerate. A few mixed sulfur–carbon clusters also belong to this category, namely,  $C_3S_3$  and  $C_2S_4$  (Figs. 8, 10).

Third, the geometry is drastically changed after ionization. The latter situation appears when the ground-state geometry of the neutral species does not correspond to any local minimum on the PES of the monopositive ion. We find typical examples in the pure phosphorus cluster family. For instance, when ionized, the tetrahedral  $P_4$  rearranges without activation to the global minimum of  $P_4^+$ , that is, the puckered ring-shaped form (<sup>2</sup>B<sub>1</sub>, structure XVII). Distortion to lower symmetry ( $T_d \rightarrow C_{2\nu}$ ) causes considerable stabilization in this molecule (tetrahedral  $P_4^+$  possesses three imaginary frequencies and is a saddle point of higher order on the PES). Another case of interest is the pure phosphorus cluster P<sub>5</sub>. The neutral P<sub>5</sub> is a distorted tetrahedral P<sub>4</sub> edge capped by an additional phosphorus. After ionization, this structure directly evolves toward the global minimum of P<sub>5</sub><sup>+</sup>, that is a perfect tetragonal pyramid (<sup>1</sup>A<sub>1</sub>, structure XVIII). Likewise, the neutral P<sub>6</sub> prefers a V-like arrangement of nuclei, which ultimately distorts to the puckered double-T-shaped configuration of the corre-



Fig. 10. Ground-state geometries of neutral  $C_n S_p$  (n + p = 3-6) clusters. B3LYP/6-311G\* total energies (in hartree) are displayed under each structure.

sponding cation  $P_6^+$  (<sup>2</sup> $A_g$ , structure XXIV), the V-like arrangement of nuclei (<sup>2</sup> $A_1$ , structure XV) being a saddle point on the PES of  $P_6^+$ .

### 4. Conclusion

A comparative study of cations  $C_n X_p^+$  (X = P, S; n + p = 3-6) has been presented. General tendencies were derived as for the structural properties of these clusters. In particular, building-up patterns of medium-sized  $C_n X_p^+$  clusters can be set up on a few simple rules, the most important being that CC bonds are favored over CX bonds that and XX bonds are avoided in mixed clusters. In carbon-rich structures, the heteroatoms (S or P) occupy the outermost positions relative to the pure carbon substructure. Because of the multivalence of phosphorus, the phosphorusrich clusters can adopt various ground-state geometries. Besides, S remains divalent in mixed sulfur– carbon structures, strongly limiting the number of bonds that sulfur can form. As a matter of fact, sulfur-rich clusters very often appear in the form of Van der Waals complexes, and pure sulfur clusters are either rings  $(S_4^+, S_6^+)$  or open chains  $(S_3^+, S_5^+)$ . Regarding the role of the charge in the relative stability of the atomic arrangement, either pure phosphorus or pure sulfur compounds (except S<sub>3</sub> and S<sub>6</sub>) and a number of mixed sulfur–carbon clusters, namely, C<sub>3</sub>S<sub>3</sub>, C<sub>2</sub>S<sub>4</sub>, and CS<sub>5</sub>, adopt distinct geometries depending on whether each of these clusters is in its neutral or ionic form. This result is important in mass spectrometry techniques where the cluster is ionized before observation and measurement.

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